

Written Round: February 25, 2023 at Regional Testing Sites Ciphering Round: April 15, 2023 at University of North Alabama

ALGEBRA II EXAMINATION

Construction of this test directed by Ashley Johnson, University of North Alabama

INSTRUCTIONS

This test consists of 50 multiple choice questions. The questions have not been arranged in order of diculty. For each question, choose the best of the ve answer choices labeled A, B, C, D and E. A calculator is NOT permitted.

The test will be scored as follows: 5 points for each correct answer, 1 point for each question left unanswered and 0 points for each wrong answer. (Thus a \perfect paper" with all questions answered correctly earns a score of 250, a blank paper earns a score of 50, and a paper with all questions answered incorrectly earns a score of 0.)

Random guessing will not, on average, either increase or decrease your score. However, if you can eliminate one or more of the answer choices as wrong, then it is to your advantage0ri7 17e(the)-422a2ne the4(remainpherate)]TJ 0

Why Major in Mathematics?

What sorts of jobs can I get with a mathematics degree? Examples of occupational opportunities available to math majors:

Market Research Analyst Cryptanalyst Mathematician
Air Tra c Controller Professor Meteorologist
Climate Analyst Pollster Medical Doctor

Estimator Population Ecologist Lawyer
Research Scientist Operations Research Actuary
Computer Programmer Data Mining Statistician

Where can I work? What sorts of companies hire mathematicians? Well just to name a few...

U.S. Government Agencies such as the National Center for Computing Sciences, the National Institute of Standards and Technology (NIST), the National Security Agency (NSA), and the U.S. Department of Energy.

Government labs and research o ces such as Air Force O ce of Scienti c Research, Los Alamos National Laboratory, and Sandia National Laboratory.

Engineering research organizations such as AT&T Laboratories - Research, Exxon Research and Engineering, and IBM Research.

Computer information and software rms such as Adobe, Google, Mentor Graphics, Microsoft, and Yahoo Research.

Electronics and computer manufacturers such as Alcatel-Lucent, Hewlett-Packard, Honeywell, Philips Research, and SGI.

Aerospace and transportation equipment manufacturers such as Boeing, Ford, General Motors, and Lockheed Martin.

Transportation service providers such as FedEx Corporation and United Parcel Service (UPS).

Financial service and investment manangement rms such as Citibank, Morgan Stanley, and Prudential.

A Mathematics Major isn't just for those wanting to be Mathematicians!

The top scoring major on the Law School Entrance Exam (LSAT) is Mathematics (Source: Journal of Economic Education)

Mathematics is also a top 5 scoring major on the Medical School Entrance Exam (MCAT) (Source: American Institute of Physics)

Study in the eld of mathematics o ers an education with an emphasis on careful problem solving, precision of thought and expression, and the mathematical skills needed for work in many other areas. Many important problems in government, private industry, and health and environmental elds require mathematical techniques for their solutions. The study of mathematics provides species analytical and quantitative tools, as well as general problem-solving skills, for dealing with these problems.

١.	perpendicular to it through the point $(1;1)$.						
	(A) $\frac{7}{6}$	(B) $\left[\frac{17}{6}\right]$	(C) $\frac{23}{6}$	(D) $\frac{25}{6}$	(E) None of these		
2.	If (a; b) is a solution	on to the system be	ow, nd the smalle	est possible value of a	+ <i>b</i> .		
	$\stackrel{\text{S}}{\geqslant} \frac{1}{x^2} \frac{3}{y^3} =$						
	$\stackrel{\geqslant}{\cdot} \frac{2}{x^2} \frac{1}{y^3} =$	7					
	(A) $\left[\frac{1}{2}\right]$	(B) $\frac{3}{4}$	(C) $\frac{3}{2}$	(D) $\frac{5}{4}$	(E) None of these		
3.	The rst and fth	terms of an arithme	etic sequence are	3 and 17, respectively.	Find the 50th term.		
	(A) 193	(B) 242	(C) 247	(D) 977	(E) None of these		
4.	Simplify $\frac{1}{3} + 5^{C}$	0.07 108 .					
	(A) $\frac{11^{D} \overline{3}}{3}$	(B) $ \frac{5^{\frac{7}{3}}}{3} $	(C) $\frac{13^{0}\overline{3}}{3}$	(D) $\frac{25^{1/3}}{3}$	(E) None of these		
5.	(value of twenty		re the same numb	nts), dimes (value of tel er of nickels as dimes.			
	(A) 23	(B) 25	(C) 29	(D) 31	(E) None of these		
6.	Which of the follow	wing pairs (a; x) is a	a solution to the ed	quation			
			$\frac{4a+x}{a+x} 1 = \frac{1}{3a}$				
	(A) $(^{\mathcal{O}}_{\overline{5}}; 3^{\mathcal{O}}_{\overline{5}})$	(B) $(3^{D}\overline{5};^{D}\overline{5})$	(C) $(^{\mathcal{D}}_{\overline{5};3}^{\mathcal{D}}_{\overline{5}})$	(D) $ \left[(3^{\cancel{5}}\overline{5};^{\cancel{5}}\overline{5}) \right] $	(E) None of these		
7.	Find the positive r	real solution to the	equation $2x^2 = 3x^6$	$9x^{2=5} = 0.$			
	(A) $3^{\sqrt[3]{3}}$	(B) $\frac{3^{\frac{12}{3}}}{4}$	(C) $^{p}\overline{81}$	(D) $\frac{P_{\overline{162}}}{2}$	(E) None of these		

8. Find the sum of the reciprocals of the two solutions to the equation (2x 3)(x 4) = 33.

(A) $\frac{55}{666}$ (B) $\frac{39}{74}$ (C) $\frac{2}{5}$ (D) $\boxed{\frac{11}{21}}$ (E) None of these

9. If a is the largest real solution to the equation $(x^2 x + 2)^2 + 2(x 5)(x + 4) = 36$, $d^3 4a + 2$.

(**A**) 2 (**B**) 17

30. Use the fact that $\log_{10} 2$ 0:301 to nd the approximate value of $\log_{10} 50$.

- **(A)** 0:7525
- **(B)** 1.301
- (C) 1.505
- **(D)** 1.699

(E) None of these

31. Let $f(x) = 2x^3 - 6x^2 + 6x$ 18 and $g(x) = x^2 + 4$. When x = 80, what is the positive remainder when f(x) is divided by g(x)?

- (**A**) 18
- (B) 154
- (C) 6250
- (**D**) 6404

(E) None of these

32. Find the value of $\frac{(5+i)(2-2i)}{3-2i}$ where *i* is the imaginary unit.

- **(A)** 2
- **(B)** 2
- (C) 2 + 2i
- (**D**) 2 2*i*

(E) None of these

49. If $x^2 + 2x + 5$ is a factor of $x^4 + px^2 + q$, then what is p + q?

(**A**) 10

(B) 19

(**C**) 26

(**D**) 31

(E) None of these

50. Trent is preparing a salad. He can make his salad with just lettuce, or he can make it with lettuce and any of the following toppings: cucumbers, tomatoes, onions, carrots, mushrooms, croutons, and/or cheese. How many variations of the salad are possible?

(A) 49

(B) 64

(C) 128

(D) 256

(E) None of these